EC 6303-SIGNALS & SYSTEMS

UNIT I

CLASSIFICATION OF SIGNALS AND SYSTEMS

1. Define Signal.

Signal is a physical quantity that varies with respect to time, space or a n y other independent variable.(Or)

It is a mathematical representation of the system

Eg $y(t) = t$. and $x(t) = \sin t$.

2. Define system.

A set of components that are connected together to perform the particular task.

3. What are the major classifications of the signal?

(i) Discrete time signal

(ii) Continuous time signal

4. Define discrete time signals and classify them.

Discrete time signals are defined only at discrete times, and for these signals, the independent variable takes on only a discrete set of values.

Classification of discrete time signal:

1. Periodic and A periodic signal

2. Even and Odd signal

5. Define continuous time signals and classify them.

Continuous time signals are defined for a continuous of values of the independent variable. In the case of continuous time signals the independent variable is continuous.

For example:

(i) A speech signal as a function of time

(ii) Atmospheric pressure as a function of altitude

Classification of continuous time signal:

(i) Periodic and A periodic signal

(ii) Even and Odd signal

6. Define discrete time unit step &unit impulse.(APRIL/MAY 2011) .(NOV/DEC-2014)

Discrete time Unit impulse is defined as

$$\delta[n]= \begin{cases} 0, & n \neq 0 \\ 1, & n=0 \end{cases}$$

Unit impulse is also known as unit sample.

Discrete time unit step signal is defined by

$$U[n]=\begin{cases} 0, & n=0 \\ 1, & n \geq 0 \end{cases}$$

7. Define continuous time unit step and unit impulse.

Continuous time unit impulse is defined as

$$\delta(t) = \{1, t=0$$
$$\{0, t \neq 0$$

Continuous time Unit step signal is defined as

$$U(t) = \{0, t<0$$
$$\{1, t \geq 0$$

8. Define unit ramp signal. (APRIL/MAY 2011)

Continuous time unit ramp function is defined by $r(t) = \{0, t<0$

$$\{t, t \geq 0$$

A ramp signal starts at t=0 and increases linearly with time 't'.

9. Define periodic signal. and nonperiodic signal.

A signal is said to be periodic, if it exhibits periodicity.i.e., $X(t+T) = x(t)$, for all values of t.

Periodic signal has the property that it is unchanged by a time shift of T.

A signal that does not satisfy the above periodicity property is called an aperiodic signal.

10. Define even and odd signal ? (MAY/JUNE 2010)

➤ A discrete time signal is said to be even when, $x[-n] = x[n]$. The continuous time signal is said to be even when,

$$x(-t) = x(t)$$

For example, $\cos\omega n$ is an even signal.

➤ The discrete time signal is said to be odd when $x[-n] = -x[n]$. The continuous time signal is said to be odd when $x(-t) = -x(t)$

Odd signals are also known as non symmetrical signal. Sine wave signal is an odd signal.

11. Define Energy and power signal. (APRIL/MAY 2011 &15)

➤ A signal is said to be energy signal if it have finite energy and zero power.

➤ A signal is said to be power signal if it have infinite energy and finite power.

➤ If the above two conditions are not satisfied then the signal is said to be neigther energy nor power signal

12. Define unit pulse function.

Unit pulse function (t) is obtained from unit step signals

$$u(t) = u(t+1/2) - u(t-1/2)$$

The signals $u(t+1/2)$ and $u(t-1/2)$ are the unit step signals shifted by 1/2units in the time axis towards the left and right ,respectively.

13. Define continuous time complex exponential signal.

The continuous time complex exponential signal is of the form $x(t)=Ce^{at}$ where c and a are complex numbers.

14. What is continuous time real exponential signal.

Continuous time real exponential signal is defined by $x(t)=Ce^{at}$ Where c and a are complex numbers. If c and a are real ,then it is called as real exponential.

15. What is continuous time growing exponential signal?

Continuous time growing exponential signal is defined as $x(t)=Ce^{at}$,Where c and a are complex numbers.

If a is positive,as t increases , then x(t) is a growing exponential.

16. What is continuous time decaying exponential?

Continuous time growing exponential signal is defined as $x(t)=Ce^{at}$

Where c and a are complex numbers.

If a is negative, as t increases, then x(t) is a decaying exponential.

17. What are the types of Fourier series?

1. Exponential Fourier series
2. Trigonometric Fourier series

18. Write down the exponential form of the Fourier series representation of a Periodic signal?
(MAY/JUNE2012)

$x(t) = a_k e^{jk\omega_o t}$ Here the summation is taken from - to .

$a_k = 1/T\ x(t)e^{-jk\omega_o t}$ Here the integration is taken from 0 to T.

The set of coefficients { a_k } are often called the Fourier series coefficients or spectral

coefficients.

The coefficient a_o is the dc or constant component of x(t).

19. Write down the trigonometric form of the Fourier series representation of a periodic signal?

$x(t) = a_o + [a_n \cos n\omega_o t + b_n \sin n\omega_o t\ ]$

where

$a_o = 1/T\ x(t)\ dt$

$a_n = 1/T\ x(t)\cos n\omega_o t\ dt$

$b_n = 1/T\ x(t)\cos n\omega_o t\ dt$

20. Write short notes on dirichlets conditions for fourier series.

➢ x (t) must be absolutely integrable

➢ The function x(t) should be single valued within the interval T.

➢ The function x(t) should have finite number of discontinuities in any Finite interval of time T.

➢ The function x(t) should have finite number of maxima &minima in the interval T.

21. State Time shifting property in relation to Fourier series.

$$x(t-t_0) \xrightarrow{FS} a_k e^{-jk\omega_0 t}$$

Time shifting property states that; when a periodic signal is shifted in time, the magnitudes of its Fourier series coefficients remain unaltered.

22. State parseval's theorem for continuous time periodic signals.

Parseval's relation for continuous time periodic signals is

$$1/T \quad x(t)^2 \quad dt = a \qquad k$$

Parseval's relation states that the total average power in a periodic signal equals the sum of the average power in all of its harmonic components.

UNIT II

ANALYSIS OF CONTINUOUS TIME SIGNALS

1. Define continuous time system.

A continuous time system is a system in which continuous time input signals are applied and result in continuous time output signals.

2. Define Fourier transform pair.

Consider the aperiodic signal x(t) &Fourier transform of x(t) is defined as

$$X(j\omega) = \quad x(t) \ e^{-j\omega t} \ dt \ \text{-------------(1)} \quad \text{Inverse}$$

fourier transform of x(t) is given by

$$x(t) = 1/2\pi \quad X(j\omega) e^{j\omega t} \ d\omega \ \text{------(2)}$$

Equations (1)& (2) are referred to as the fourier transform pair.

3. Write short notes on dirichlets conditions for Fourier transform. (JUNE 2010)

➢ x (t) be absolutely integrable

➢ x (t) have a finite number of maxima and minima within any finite interval.

➢ x(t) have a finite number of discontinuities within any finite interval. Furthermore each of these discontinuities must be finite.

4. Explain how aperiodic signals can be represented by Fourier transform.

Consider the aperiodic signal x(t) &Fourier transform of x(t) is defined as

$$X(j\omega) = \quad x(t) \ e^{-j\omega t} \ dt \ \text{-------------(1)} \quad \text{Inverse}$$

fourier transform of x(t) is given by

$$x(t) = 1/2\Pi \quad X(j\omega) e^{j\omega t} \ d\omega \ \text{------(2)}$$

5. State convolution property in relation to fourier transform. .(APRIL/MAY 2011)

Y(t)=x(t)*h(t)

Y(jω)= H(jω)X(jω)   Convolution property states that convolution in time domain corresponds to multiplication in the frequency domain.

6. State parseval's relation for continuous time fourier transform. (APRIL 2011)

If x(t) and X(jω) are a fourier transform pair then $x(t)^2$ dt = 1/2 πi |X(j ω)|2 dω

7. What is the use of laplace transform?(DECEMBER 2009)

Laplace transform is another mathematical tool used for analysis of signals and systems.Laplace transform is used for analysis of unstable systems.

8. What are the types of Laplace transform?

1. Bilateral or two sided Laplace transform.

2. Unilateral or single sided Laplace transform.

9. Define Bilateral and unilateral Laplace transform.

The bilateral Laplace transform is defined as

$X(s)=x(t)e^{-st}dt$

Here the integration is taken from - t o . Hence it is called bilateral Laplace Transform.

The unilateral Laplace transform is defined as

$X(s)=x(t)e^{-st}dt$

Here the integration is taken from 0 to .Hence it is called unilateral laplace Transform.

10. Define inverse Laplace transform.

The inverse Laplace transform is given as

$x(t)=1/2\pi j$ X(s) $e^{st}ds$

Here the integration is taken from σ-j to σ+j .

11. State the linearity property for Laplace transforms.

Let x1(t)◄────► X1(S) and

x2(t) ◄────► X2(s) be the two Laplace transform pairs.Then linearity property

states that

$L[a1x1(t)+a2x2(t)]=a1X_1(s)+a2X_2(s)$,Here a1 and a2 are constants.

12. State the time shifting property for Laplace transforms.(MAY/JUNE2012)

Let x(t) ◄────► X(S) be a laplace transform pair.If x(t) is delayed by time t0 ,then its laplace transform is multiplied by e^{-st0}.

$L[x(t-t0)=e^{-st0} X(s)$

13. Region of convergence of the Laplace transforms.

The range of values of s for which the integral i.e., $x(t)e^{-st}dt$ converges is referred to as the region of convergence of the laplace transform.

14. What is pole zero plot.

The representation of $X(s)$ through its poles and zeros in the splane is referred to as pole zero plot.

15. State initial value theorem and final value theorem for laplace transform.(APRIL2011)MAY/JUNE(2012)

➢ If $L[x(t)]=X(s)$, then initial value theorem states that $x(0)=\lim(s\text{--->}\ )\ SX(S)$

➢ If $L[x(t)]=X(s)$, then final value theorem states that $\lim(t\text{--->}\ )\ x(t)=\lim(s\text{--->}0)\ SX(S)$

16. State Convolution property.

The laplace transform of convolution of two functions is equivalent to multiplication of their laplace transforms.

$$L[x1(t)*x2(t)]=X_1(s)X_2(s)$$

17. Define a causal system.(APRIL/MAY 2015)

The causal system generates the output depending upon present &past inputs only. A causal system is non anticipatory.

18. What is meant by linear system?

A linear system should satisfy superposition principle. A linear system should satisfy $F[ax_1(t)+bx_2(t)] \rangle a\ y\ _1(t)+by_2(t)$

$$y1(t)=F[x_1(t)]$$
$$y2(t)=F[x_2(t)]$$

19. Define time invariant system.

➢ A system is time invariant if the behavior and characteristics of the system are fixed over time.

➢ A system is time invariant if a time shift in the input signal results in an identical time shift in the output signal.For example, a time invariant system should produce y(t-t0)as the output when x(t-to) is the input.

20. Define stable system.(APRIL/MAY 2015)

When the system produces bounded output for bounded input, then the system is called bounded input& bounded output stable.If the signal is bounded, then its magnitude will always be finite.

21. Define memory and memory less system.

The output of a memory system at any specified time depends on the inputs at that specified time and at other times. Such systems have memory or energy storage elements.

The system is said to be static or memory less if its output depends upon the present input only.

22. Define invertible system.

A system is said to be invertible if the input is get from the output input. Otherwise the system is noninvertible system.

23. What is superposition property?

If an input consists of the weighted sum of several signals, then the output is the superposition that is, the weighted sum of the responses of the system to each of those signals

UNIT III

LINEAR TIME INVARIANT –CONTINUOUS TIME SYSTEMS

1 . Why CT signals are represented by samples? (APRIL/MAY 2015)

➢ A CT signal can not be processed in the digital processor or computer.

➢ To enable the digital transmission of CT signals.

2. What is meant by sampling?

A sampling is a process by which a CT signal is converted into a sequence of discrete samples with each sample representing the amplitude of the signal at the particular instant of time.

3. State Sampling theorem. .(MAY/JUNE 2010)

➢ A band limited signal of finite energy, which has no frequency components higher than the W hertz, is completely described by specifying the values of the signal at the instant of time separated by 1/2W seconds and

➢ A band limited signal of finite energy, which has no frequency components higher than the W hertz, is completely recovered from the knowledge of its samples taken at the rate of 2W samples per second.

4. What is meant by aliasing?

When the high frequency interferes with low frequency and appears as

Low then the phenomenon is called aliasing.

5. What are the effects aliasing?

Since the high frequency interferes with low frequency then the distortion is generated.

The data is lost and it cannot be recovered.

6. How the aliasing process is eliminated.

i). Sampling rate f_S 2W.

ii). strictly band limit the signal to 'W'.

This can be obtained by using the Low pass filer before the sampling process. It is also called as ant aliasing filter.

7. Define Nyquist rate. and Nyquist interval. .(MAY/JUNE 2012)

➢ When the sampling rate becomes exactly equal to '2W'samples/sec, for a given bandwidth of W hertz, then it is called Nyquist rate.

➢ Nyquist interval is the time interval between any two adjacent samples. Nyquist rate = 2W Hz

> Nyquist interval = 1/2W seconds.

8. Define sampling of band pass signals.

A band pass signal x(t) whose maximum bandwidth is '2W' can be completely represented into and recovered from its samples, if it is sampled at the minimum rate of twice the band width.

9. Define Z transform. .(MAY/JUNE 2010)

The Z transform of a discrete time signal x[n] is denoted by X(z) and it is given as

$X(z) = x[n] z^{-n}$.and the value n range from - to + . Here 'z' is the complex variable.This Z transform is also called as bilateral or two sided Z transform.

10. What are the two types of Z transform?

(i) Unilateral Z transforms

(ii) Bilateral Z transforms

11. Define unilateral Z transform.

The unilateral Z transform of signal x[n] is given as

$X(z) = x[n] z^{-n}$

The unilateral and bilateral Z transforms are same for causal signals.

12. What is region of Convergence?

The region of convergence or ROC is specified for Z transform, where it Converges.

13. What are the Properties of ROC? (APRIL/MAY 2008)

> The ROC of a finite duration sequence includes the entire z- plane, except z= 0 and |z|= 1.

> ROC does not contain any poles.

> ROC is the ring in the z-plane cantered about origin.

> ROC of causal sequence (right handed sequence) is of the form |z| > r. v. ROC of left handed sequence is of the form |z| < r.

> ROC of two sided sequence is the concentric ring in the z plane.

14. What is the time shifting property of Z transform?

x[n] ⟷ X(Z) then

x[n-k] ⟷ Z^{-k} X[Z].

15. What is the differentiation property in Z domain?

x[n] ⟷ X(Z) then

nx[n] ⟷ -z d/dz{X[Z].}.

16. State convolution property of Z transforms. (APRIL/MAY 2011)/JUNE 2010

The convolution property states that if x_1[n] X_1(Z) and

X_1[n] ⟷ X_1(Z)

x_2[n] ⟷ X_2(Z) then

x_1[n] *x_2[n] ⟷ X_1(Z) X_2(Z)

That is convolution of two sequences in time domain is equivalent to multiplication of their Z transforms.

17. State the methods to find inverse Z transform. .(APRIL/MAY 2015)

- ➤ Partial fraction expansion
- ➤ Contour integration
- ➤ Power series expansion
- ➤ Convolution method.

18. State multiplication property in relation to Z transforms.

This property states that if , $x_1[n]$ $X_1(Z)$ nd

$X_1[n]$ $\longleftrightarrow$ $X_1(Z)$

$x_2[n]$ $\longleftrightarrow$ $X_2(Z)$ then

$x_1[n] \, x_2[n]$ $\longleftrightarrow$ $1/2\Pi j$ $X_1(v). X_2(Z/v)v^{-1}dv$

Here c is a closed contour .It encloses the origin and lies in the Roc which is common to both

$X_1(v). X_2(1/v)$

19. State parseval's relation for Z transforms.

If $x_1[n]$ and $x_2[n]$ are complex valued sequences, then the parseval's relation states that

$x_1[n] \, x_2^*[n] = 1/2\Pi j$ $X_1(v). X_2^*(1/v^*)v^{-1}dv.$

20. What is the relationship between Z transform and Fourier transform?

$X(z) = x[n] \, z^{-n}.$------------------1.

$X(w) = x[n]e^{-j\omega n}.$----------------2

$X(z)$ at $z = e^{j\omega}$ is = X (w).

When z- transform is evaluated on unit circle (ie.$|z| = 1$) then it becomes Fourier transform.

UNIT IV

ANALYSIS OF DISCRETE TIME SIGNALS

1. What is meant by step response of the DT system?

The output of the system y(n) is obtained for the unit step input u(n) then it is said to be step response of the system.

2. Define Transfer function of the DT system.

The Transfer function of DT system is defined as the ratio of Z transform of the system output to the input. That is ,$H(z) = Y(z)/X(z)$.

3. Define impulse response of a DT system. (APRIL/MAY 2011)

- The impulse response is the output produced by DT system when unit impulse is applied at the input. The impulse response is denoted by h(n).
- The impulse response h(n) is obtained by taking inverse Z transform from the   transfer function H(z).

4. .State the significance of difference equations.

The input and output behaviour of the DT system can be characterized with the help of linear constant coefficient difference equations.

5. Write the difference equation for Discrete time system.

The general form of constant coefficient difference equation is

$$Y(n) = -\Sigma\, a_k\, y(n-k) + \Sigma\, b_k\, x(n-k)$$

Here n is the order of difference equation.x(n) is the input and y(n) is the output.

6. Define frequency response of the DT system.

The frequency response of the system is obtained from the Transfer function by replacing $z = e^{j\omega}$

Ie, $H(z)=Y(z)/X(z)$, Where $z = e^{j\omega}$

7. What is the condition for stable system?

A LTI system is stable if

$\Sigma_|h(n)_| < \infty$.

Here the summation is absolutely summable

8. What are the blocks used for block diagram representation?.

The block diagrams are implemented with the help of scalar multipliers, adders and multipliers

9. State the significance of block diagram representation.

The LTI systems are represented with the help of block diagrams. The block diagrams are more effective way of system description. Block Diagrams Indicate how individual calculations are performed. Various blocks are used for block diagram representation.

10. What are the properties of convolution?

i.Commutative

ii.Assosiative.

iii.Distributive

11. State the Commutative properties of convolution?

Commutative property of Convolution is

$x(t)*h(t)=h(t)*x(t)$

12. State the Associative properties of convolution

Associative Property of convolution is $[x(t)*h1(t)]*h2(t)=x(t)*[h1(t)*h2(t)]$

13. State Distributive properties of convolution

The Distributive Property of convolution is $\{x(t)*[h1(t)+ h2(t)]\}= x(t)*h1(t) + x(t)*h2(t)]$

14. Define causal system.

For a LTI system to be causal if h(n)=0,for n<0.

15. What is the impulse response of the system y(t)=x(t-t0).

Answer:

$$h(t)=\delta(t-t0)$$

16. What is the condition for causality if H(z) is given.

A discrete LTI system with rational system function H(z) is causal if and only if

i.The ROC is the exterior of the circle outside the outermost pole.

ii.When H(z) is expressed as a ratio of polynomials in z , the order of the numerator can not be greater than the order of the denominator.

17. What is the condition for stability if H(z) is given.

A discrete LTI system with rational system function H(z) is stable if and only if all of the poles

H(z) lies inside the unit circle. That is they must all have magnitude smaller than 1.

18. Check whether the system is causal or not, the H(z) is given by $(z^3 + z)/(z+1)$.

The system is not causal because the order of the numerator is greater than denominator.

19. Check whether the system is stable or not ,the H(z) is given by (z/z-a).,|a|<1.

The system is stable because the poles at z = a lies inside the unit circle.

20. Determine the transfer function for the sys tem described by the difference

equation y(n)- y(n-1) = x(n)- x(n-2). (MAY/JUNE2012)

By taking z transform on both sides the transfer function

$$H(z)=(z^2 - 1)/(z^2 - z).$$

UNIT V

LINEAR TIME INVARIANT - DISCRETE TIME SYSTEMS

1. How the discrete time system is represented.

The DT system is represented either Block diagram representation or difference equation representation.

2. What arte the classification of the system based on unit sample response?

a. FIR (Finite impulse Response) system.

b. IIR (Infinite Impulse Response) system.

3. What is meant by FIR system?(DECEMBER 2009)

If the systems have finite duration impulse response then the system is said to be FIR system.

4. What is meant by IIR system? (DECEMBER 2009)

If the system have infinite duration impulse response then the system is said to be FIR system.

5. What is recursive system? (APRIL/MAY 2008)

If the present output is dependent upon the present and past value of input then the system is said to be recursive system

6. What is Non recursive system?

If the present output is dependent upon the present and past value of input and past value of output then the system is said to be non recursssive system.

7. What is transformed structure representation?

The flow graph reversal theorem states that if the directions of all branches are reversed and positions of input and output is interchanged, the system function remain unchanged. Such structure is called transposed structure.

8. What is the difference between recursive and non recursive system?

A recursive system have the feed back and the non recursive system have no feed back .And also the need of memory requirement for the recursive system is less than non recursive system.

9. Define realization structure.

The block diagram representation of a difference equation is called realization structure. These diagrams indicate the manner in which the computations are performed.

10. What are the different types of structure realization?

i. Direct form I

ii. Direct form II

iii. Cascade form

iv. Parallel Form.

11. What is natural response?

This is output produced by the system only due to initial conditions .Input is zero for natural response. Hence it is also called zero input Response.

12. What is zero input Response?

This is output produced by the system only due to initial conditions .Input is zero for zero input response.

13. What is forced response?

This is the output produced by the system only due to input .Initial conditions are considered zero
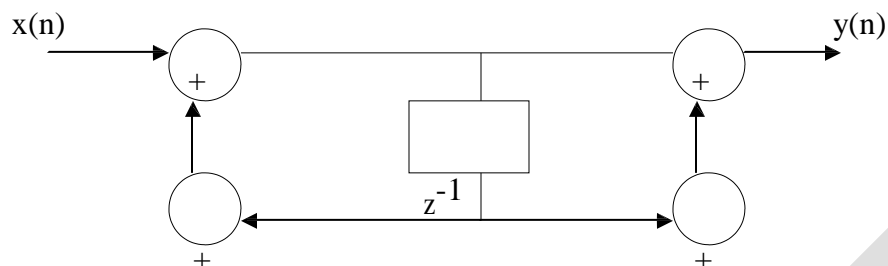
for forced response. It is denoted by $y^{(f)}(t)$.

14. **What is complete response**?

The complete response of the system is equal to the sum of natural response and forced response .Thus initial conditions as well as input both are considered for complete response.

15. Give the direct form I structure.
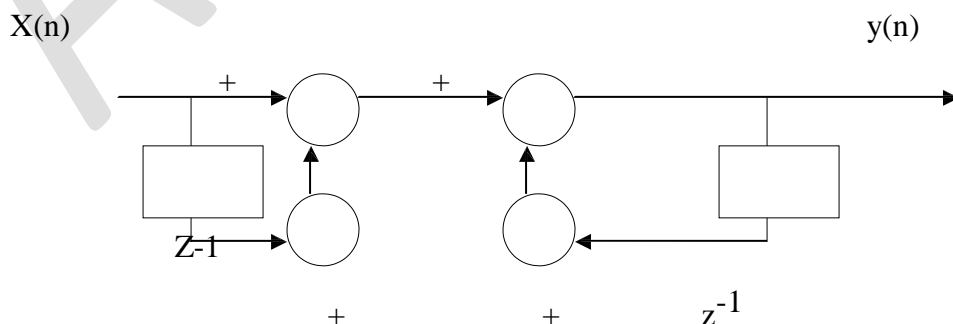
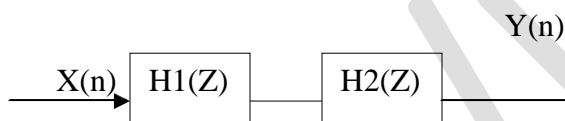**16. Give the direct form II structure.** . (MAY/JUNE 2012)

17. How the Cascade realization structure obtained..

The given transfer function H(z) is spilited into two or more sub systems.

That is for eg.

H(z) = H$_1$(z) H$_2$(z)

UNIT-I (Important 16 marks)

1. Explain all classification of signals with Examples for Each Category.

2. Determine the whether the systems described i/p and o/p equations are causal, linear, time invariant, dynamic and stable.

   i) $y_1(t) = x(t-3) + (3-t)$ ii) $y_2(t) = \frac{dx(t)}{dt}$ iii) $y_3[n] = nx_1[n] + bx_2[n]$ iv)

   $Eve\{x[n-1]\}$

3. Distinguish between the following.

   i) Continuous time signal and discrete time signal   ii) Unit step and Unit Ramp functions.

   iii) Periodic and Aperiodic Signals.   iv) Deterministic and Random Signals.

4. Define LTI system. List the properties of LTI system and explain.

5. Determine whether the following systems are linear or not.

   i) (dy(t)/dt)+3ty(t)= t^2x(t)   ii) y(n)= 2 x(n) +1/x(n-1).

6. Determine whether the following signal is periodic. If periodic, determine the fundamental period

   i) x(t) =3cost +4cos(t/3).   ii) x(t)=sin 20πt +sin 5πt.

7. Write about elementary Continuous time Signals in Detail.

UNIT-II

1. State and prove the properties of Fourier Transform.

2. State and prove the properties of Laplace Transforms.

3. State and Prove the properties of Fourier series

4. Obtain Trigonometric Fourier series for the full wave rectified sine wave.

5. Obtain the inverse Laplace transform of the function x(s)=1/($s^2 + 3s + 2$),ROC:-2<Re{s}<-1.

6. Write the properties of ROC of Laplace transform.

7. Find the Laplace transform of the signal f(t)= $e^{-at}sin\omega t$**.**

8. Find the Fourier transform of the signal x(t)= $e^{-a|t|}$.

UNIT-III

1. Explain the properties of convolution integral.

2. The system produced the output y(t)= e^{-t}u(t) for an input x(t)= e^{-2t}u(t) .Determine

   i) Frequency response   ii) magnitude and phase of the response   iii) the impulse response.

3. Determine the impulse response h(t) of the system given by the differential equation $\frac{d^2y(t)}{dt^2} + \frac{3dy(t)}{dt} + 2y(t) = x(t)$.with all initial conditions to be zero.

4. Obtain the direct form-I realization of $\frac{d^2y(t)}{dt^2} + \frac{5dy(t)}{dt} + 4y(t) = \frac{dx(t)}{dt}$.

5. A stable LTI system is characterized by the differential equation $\frac{d^2y(t)}{dt^2} + \frac{4dy(t)}{dt} + 3y(t) = \frac{dx(t)}{dt} + 2x(t)$.Find the frequency response & Impulse response using Fourier transform.

6. Draw DF-I, cascade form & parallel form of a system with system function, H(s)=1/(s+1) (s+2).

7. Compute & plot the convolution y(t) of the given signals.

   i) X(t)=u(t-3) – u(t-5) , h(t)=u(t)

   ii) X(t)=u(t) , h(t)= u(t).

8. What is Impulse Response? Show that the Response of an LTI system is convolution Integral of its impulse Response with input signal?

9. Using Laplace transform, find the impulse response of an LTI system described by the differential equation. $\frac{d^2y(t)}{dt^2} - \frac{dy(t)}{dt} - 2y(t) = x(t)$.

UNIT-IV

1. Prove the sampling theorem and explain how the original signal can be reconstructed from the sampled version.

2. State & explain Properties of DTFT.

3. State and prove properties of Z transform.

4. Find the inverse Z Transform of $X(z) = 1/(1-0.5z^{-1} + 0.5z^{-2})$ for ROC $|Z| > 1$.

5. Determine the transfer function and impulse response for the causal LTI system described by the equation using Z transform $Y(n) - 1/4y(n-1)-3/8y(n-2) = -x(n) + 2x(n-1)$.

6. Determine the Z transform and ROC of the sequence $x(n) = a^n \cos(\omega n)u(n)$.

7. Determine the DTFT of $(\frac{1}{2})^n$ u (n). Plot its spectrum.

8. Determine the discrete time Fourier transform of $x(n)=a^{\|n\|}, \| a \| < 1$.

UNIT-V

1. Discuss the block diagram representation for LTI discrete time systems.

2. Obtain the cascade and parallel form realization of the following system $y(n)-1/4y(n-1)-1/8y(n-2)= x(n)+3x(n-1)+2x(n-2)$.

3. Obtain the discrete form II structure for $y(n)-3/4y(n-1)+1/8y(n-2)=x(n)+1/2x(n-1)$.

4. Draw direct form I and direct form II implementations of the system described by equation.

   $y(n)+1/4y(n-1)+1/8y(n-2)= x(n)+x(n-1)$.

5. Draw the direct form, cascade form and parallel form block diagrams of the following system function.

   $H(z)=1/(1+(1/2) z^{-1}) (1-(1/4) z^{-1})$.

6. Find the impulse response of the discrete time system described by the difference equation

   $y(n-2)-3y(n-1)+2y(n)=x(n-1)$.

7. The system function of the LTI system is given as $H(Z)= (3-4z^{-1}) / (1-3.5Z+1.5z^2)$.Specify the ROC of H(Z) and determine h(n) for the following condition (1) stable system   (2) causal system.

8. Determine the system function and impulse response of the causal LTI system. Defined by the difference equation $y(n)-1/2y(n-1)+1/4y(n-2)=x(n)$ Using Z transform, determine y(n) if x(n)=u(n).

9. Compute convolution sum of the following sequences

   $x(n)=\begin{cases} 1, & 0 \leq n \leq 4 \\ 0, & otherwise \end{cases}$, $h(n)=\begin{cases} a^n, & 0 \leq n \leq 6 \\ 0, & otherwise \end{cases}$.

10. Compute the response of the system $y(n)=0.7y(n-1)-0.12y(n-2)+ x(n-1)+x(n-2)$ to the input $x(n)=nu(n)$.Is the system stable?